Applications play an important role in the reliability evaluation of communication networks. In other words, the reliability of a network can be totally different when different applications are considered for the same network. However existing reliability evaluation methods, which are mostly based on the graph theory, give no or little consideration to applications. This paper proposes a concept of network application reliability and a Markov-based method for analyzing the proposed network application reliability measure. Furthermore, based on the reliability of each individual application, a method is proposed to evaluate the overall network reliability that incorporates effects of different applications running on the network. Both a case study and experiments are performed to illustrate the proposed concept and methods.

**Keywords:** application, Markov model, network, reliability.

Aplikacje odgrywają ważną rolę w ocenie niezawodności sieci komunikacyjnych. Innymi słowy, niezawodność sieci może być całkowicie różna dla różnych aplikacji tej samej sieci. Niestety, istniejące metody oceny niezawodności, w większości oparte na teorii grafów, poświęcają niewiele lub nie poświęcają wcale uwagi aplikacjom. W niniejszym artykule przedstawiono koncepcję niezawodności aplikacji sieciowych oraz opartą na modelu Markowa metodę analizy proponowanej miary niezawodności aplikacji sieciowych. Ponadto, na podstawie niezawodności poszczególnych aplikacji, zaproponowano metodę oceny ogólnej niezawodności sieci, która łączy efekty różnych aplikacji działających w danej sieci. Zaproponowaną koncepcję i metody omówiono na podstawie studium przypadku oraz badań eksperymentalnych.

**Słowa kluczowe:** aplikacja, model Markowa, sieć, niezawodność.

1. Introduction

Reliability analysis has become an essential step in the design, operation, and tuning of network systems [4, 24]. Considerable research efforts have been expended in the network reliability analysis. As a pioneer, Lee first defined and evaluated the network reliability mainly based on network connectivity [6]. Following the similar idea, a series of network reliability evaluation algorithms and optimization methods have been proposed [1, 3, 7, 8, 9, 12, 13, 19, 20, 21, 23, 28, 30, 32]. All these studies are based on the graph theory and the network topology. Among these works, synthesis evaluation methods are especially discussed in [1, 7, 8, 28, 30]. Later on other more advanced synthesis evaluation methods have been proposed, including but not limited to AHP (Analytic Hierarchy Process) [14, 27], fuzzy reliability evaluation [17], and ANN (Artificial Neural Network) [5]. Since 1980s, network congestion and traffic delay have become noticeable factors in the network reliability research. For example, Barberis and Park investigated network availability considering throughput and delay [10, 25]. Tao and Chen considered routing dynamics and congestion into the network reliability computation [33]. In general, the existing network reliability research can be classified into two types [29]: inherent reliability considering topology connectivity and applicable reliability considering network traffic. The former focuses on topology structure and has been analyzed using probability theory and graph theory. The latter focuses on how the network works and what is in the network, and examines performance reliability of the network [11, 15, 22].

Those research works on network reliability, however, gave little or no consideration to the effects of applications, though the network reliability and performance can be different when different applications run on the network. Recently, studies on application-layer network performance testing [18, 26] have started. The performance of application layer is quite different from and not directly related to the performance of the other layers in the OSI model. And end users are usually concerned with the performance of specific applications [2, 31]. It is worth noting that the Internet Engineering Task Force (IETF) proposed a performance testing methodology and some metrics on the application layer in RFC 3511 [16]. And the influence of applications for network reliability has also been noticed in [34, 35].

To the best of our knowledge, there is no work considering various applications and incorporating the effects of them in the evaluation of the network reliability. In this paper, a concept of network application reliability is proposed and a Markov-based method for analyzing the proposed application reliability measure is discussed. Furthermore, based on the reliability of each individual application, a method is proposed to evaluate the overall network reliability that considers the effects of different applications running on the network. Both a case study
and experiments are performed to illustrate the proposed concept and methods.

2. Concept and model

The following concepts are defined and used in the latter discussions:

**A network:** is a group of hardware devices and services. It has the transportation ability to support applications for users.

**A service:** is a function that a network provides to users. Usually a function is supported by a software system or a group of cooperating software systems.

**An application:** is the usage of services by a group of users with some demanded performance requirements.

**Application profile:** represents the information of an application, including information of the users involved and a set of operation probabilities of the application;

**Usage profile:** contains a set of application profiles and their occurrence probabilities.

The proposed application-centric model for communication network reliability is shown in fig.1.

![Network reliability model](image)

Fig.1. Network reliability model

Let \( R \) represent the overall network reliability, and \( R_i \) represent reliability for application \( A_i \). \( R \) is a function of \( R_i \) and usage-profile. Namely \( R \) is a function of reliabilities for all applications, and the relationship among all the applications in the network. Let \( H \) be the set of hardware that application \( A \) involves. \{\text{Feature}\} \subseteq \text{topology} \rightarrow \{\text{Reliability}\} \subseteq \text{network} \rightarrow \{\text{Transfer probabilities}\} \subseteq \text{device} \rightarrow \{\text{Reliability}\} \subseteq \text{node} \rightarrow \{\text{Reliability}\} \subseteq \text{link} \rightarrow \{\text{Reliability}\} \subseteq \text{network}.

3. Proposed algorithms

Algorithms for computing the application reliability and the overall network reliability are explained in this section. Two assumptions are made in the proposed algorithms: 1) All the network components (nodes or links) fail statistically-independently; and 2) The transfer of data flow in the network is a Markov process, meaning that the determination of the next node to transfer the flow depends on the present node, not the past path.

As briefly in Section 2, \( R \) is a function of \{\text{Feature}\}, \text{topo} \log y, \text{deploy}, and \text{app-profile}, and \( R \) is the function of \{\text{R}\} and usage-profile. The substances of the parameters in this algorithm are:

1. \{\text{Feature}\}: reliabilities of the components.
2. \text{Topo} \log y: the transfer matrix.
3. \text{Deploy}: mapping to the network components according to the deployment of the services.
4. \text{App-profile}: the transfer probability of the application when it is running.
5. \text{Usage-profile}: the number and importance of the applications.

The general algorithm can be described as the following process:

**Step 1:** prepare \{\text{Feature}\}, and \text{Usage-profile}: Analyze the network, and prepare the static parameters including the reliabilities of nodes and links from the history usage data (they usually can be obtained from devices providers). Assign the weight for each application according to its importance in the network.

**Step 2:** analyze applications on the network. For each application \( A_i \), determine its concerned services as a set \( S_i \), and its process (data flow) for the network reliability.

**Step 3:** analyze \text{deploy} for each application \( A_i \). Based on the information obtained in step2, analyze where each service is installed and what nodes and links its process concerns. Because the data flow has direction, every application \( A_i \) is mapped to two diagrams, request diagram and response diagram, corresponding to request data flow and response data flow, respectively.

**Step 4:** analyze \text{App-profile}. Acquire the multi-branch transfer probabilities of the nodes for each application \( A_i \) using history data or statistic methods for both request diagram and response diagram.

The transfer probability of a link is computed as the ratio of the size of the data flow through the link to the total size of data flows through all the links involved in the application. For example, a node used in a specific application connects with three links which are named as \( a, b, \) and \( c \), respectively. The sizes of the data flows going through the three links are respectively 20KB, 30KB and 50KB. Thus the transfer probabilities of the three links are respectively 0.2, 0.3, and 0.5.

**Step 5:** calculate reliability \( R \), for each individual application \( A_i \) using the method presented in Section 3.1.

**Step 6:** evaluate the overall network reliability using the method described in Section 3.2.

3.1. Reliability evaluation for an application

Let \( H_i \) and \( H_i' \) respectively represent the set of nodes for request diagram and response diagram of application \( A_i \), \( R_i' \)
and $R_i'$ respectively represent reliability corresponding request diagram and response diagram. There are six steps to compute the reliability of application $A_i$.

**Step 1:** obtain the transfer matrix $Q$ based on the request diagram of application $A_i$.

Let $n_i$ and $n_j$ represent network nodes, namely $n_i, n_j \in H_i^j$. Represent a link from $n_i$ to $n_j$ with $L_{i,j}$, the reliability of $n_i$ with $N_i$, the reliability of $L_{i,j}$ with $L_{i,j}$, and the transfer probability from $n_i$ to $n_j$ with $P_{i,j}$. We regard every node in the network as a state of the Markov model. The model also includes states $C$ and $F$ that represent the application request is completed successfully ($N_i=1$) and the request is failed ($N_i=0$) respectively. Thus the complete state space for the Markov model is \{$n_i, n_j, \ldots, n_n, C, F$\}.

The state transition matrix is named $T$.

$$
T = \begin{pmatrix}
N_i & 0 & 0 & \cdots & 0 & 0 \\
N_i & N_j & L_{i,j} & \cdots & 0 & 0 \\
N_i & N_i & L_{i,j} & \cdots & 0 & 0 \\
\vdots & \vdots & \vdots & \ddots & \vdots & \vdots \\
N_i & N_i & L_{i,j} & \cdots & N_i & L_{i,j} \\
C & 0 & 0 & \cdots & 0 & 0 \\
F & 0 & 0 & \cdots & 0 & 0 \\
\end{pmatrix}
$$

Where,

$$F = \sum_{j=1}^{n} N_i P_{i,j} + N_i L_{i,j} - 1 = 0 \text{ or } 1 \quad (2)$$

Every element $T(i,j)$ in matrix $T$ represents the probability of successful transfer of a flow from node $n_i$ to node $n_j$. The value of $T(i,j)$ is the product of $N_i$, $L_{i,j}$, and $P_{i,j}$. For instance, the element $T(1,2)$ in row $n_1$ and column $n_2$ is the product of the reliability of $n_1$, the reliability of $L_{1,2}$ and the transfer probability from $n_1$ to $n_2$. Namely the product of $N_i$, $L_{i,j}$ and $P_{i,j}$ represents the requester of the application whose in-degree is 0. $C$ represents the completion state and $F$ represents the failure state. Both of them are absorbing states with out-degrees of 0. Therefore, elements in the first column and the last two rows in $T$ are 0.

The matrix $Q$ is obtained by removing the row and column of $F$ from matrix $T$.

$$
Q = \begin{pmatrix}
0 & N_i & L_{i,j} & \cdots & \cdots & \cdots & 0 \\
N_i & 0 & N_i & \cdots & \cdots & \cdots & 0 \\
N_i & N_i & 0 & \cdots & \cdots & \cdots & 0 \\
\vdots & \vdots & \vdots & \ddots & \vdots & \vdots & \vdots \\
N_i & N_i & L_{i,j} & \cdots & 0 & 0 & 0 \\
C & 0 & 0 & \cdots & 0 & 0 & 0 \\
\end{pmatrix}
$$

**Step 2:** derive matrix $W$, and calculate the determinant of $W$ denoted as $|W|$. For any integer $m (m=0)$, $Q^m(i,j)$ is the probability that the data packet is transferred from $n_i$ to $n_j$ within $m$ steps. It is supposed that $S$ is a matrix with the order of $n+1$, and:

$$S = I + Q + Q^2 + \cdots + \sum_{i=0}^{n-m} Q^i$$

where, $I$ is an identity matrix.

The application reliability is thus the transfer probability from $n_i$ to $C$, that is, $R_i' = S(n_i,C)$. When $W = I - Q$, we have:

$$S = W^{-1} = (I - Q)^{-1}$$

Then the value of $|W|$ can be computed.

**Step 3:** remove the first column and the last row of $W$, name the remaining matrix as $M$, and calculate $|M|$.

**Step 4:** calculate $R_i'$ as the reliability for request diagram of application $A_i$ with the formula:

$$R_i' = (-1)^n |M| \quad (6)$$

where, $n$ is the number of nodes in the application request diagram.

**Proof:**

$$R_i' = S(n_i,C)W^{-1}(n_i,C) = \frac{W(n_i,C)}{|W|} = \frac{(-1)^{n-1}|M|}{|W|}$$

where, $W^m$ is the adjoint matrix of $W$.

**Step 5:** using the above similar steps, calculate $R_i'$ based on the response diagram for application $A_i$.

**Step 6:** compute reliability for application $A_i$ using the following formula:

$$R_i = R_i' \times R_i'^*$$

### 3.2. Reliability evaluation for the entire network

There is typically more than one application existing in the network. Therefore a method is needed to integrate the single application reliabilities to obtain the entire network reliability. In this work, the overall network reliability is evaluated as a weighted sum of reliabilities of all applications running on the network, as shown in (9).

$$R = \sum_{i=1}^{n} \omega_i R_i, \sum_{i=1}^{n} \omega_i = 1$$

Where $\omega_i$ represents the weight of application $A_i$ which indicates the number of users or the significance of the application. Consider an example where there are three applications of three groups of users called Lat1, Lan2, and Lan3 with the same significance level. The topology reliabilities of these applications are respectively \(R_1 = 0.9\), \(R_2 = 0.8\), \(R_3 = 0.9\), and the number of users of Lat1, Lan2, and Lan3 are respectively 6, 7 and 7. The weights of these applications are computed as \(\omega_1 = 6/(6+7+7) = 0.3\), \(\omega_2 = 0.35\), \(\omega_3 = 0.35\). Thus, the overall network reliability is $R = \sum_{i=1}^{3} \omega_i R_i = 0.865$.
4. Case study

In this section, a case study is performed to show how a network reliability can be evaluated using the method described in Section 3.

4.1. System description

Figure 2 illustrates a small campus network with teaching VOD (Video on Demand) applications running on it. Reliabilities of nodes and links in this network are given in table 1 and table 2, respectively. Lan1, Lan2 and Lan3 are three different groups of users. There are 10 users in Lan1, 15 in Lan2, and 25 in Lan3. Lan 1 is a LAN of student dormitories and faculty apartments; Lan 2 is a LAN of the teaching zone, and Lan 3 is a LAN of the teaching showcase area.

Service1 and Service2 are grouped together to support a VOD providing application where users can watch part of the teaching videos and TVs (referred to as application1 hereafter), and they are installed separately on Server1 and Server3. Service3 itself also supports the same VOD providing application as a main server for all the video sources (application2) and it is installed on Server2. Service4 supports a HTTP application where users access to the Internet or other communication networks (application3), and is installed on Server2 too. These three applications run on the network: users can visit application1 through Lan1, application2 through Lan2, and application3 through Lan3.

4.2. Network Reliability Evaluation

Using the method of Section 3, the reliability of this example network reliability can be evaluated using the following steps:

**Step 1:** prepare data, including reliabilities of the nodes and links, shown in tables 1 & 2.

**Step 2:** analyze applications. For example, for application1, users request Service1 (on Server1) for a special video by a browser. If this video can be provided by Service1, it can be downloaded by the users. Otherwise, the request will be transferred to Service2 (on Server3) to find the video.

For application1, \( S = \{ \text{browser, Service1, Service2} \} \). In this step, only services are analyzed without consideration of hardware, namely, these services can be installed on different servers involving different transform devices.

<table>
<thead>
<tr>
<th>Node</th>
<th>( R_i )</th>
<th>Node</th>
<th>( R_i )</th>
</tr>
</thead>
<tbody>
<tr>
<td>lan1</td>
<td>1</td>
<td>router2</td>
<td>0.97</td>
</tr>
<tr>
<td>lan2</td>
<td>1</td>
<td>router3</td>
<td>0.99</td>
</tr>
<tr>
<td>lan3</td>
<td>1</td>
<td>switch4</td>
<td>0.98</td>
</tr>
<tr>
<td>switch1</td>
<td>0.98</td>
<td>switch5</td>
<td>0.98</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Link</th>
<th>( L_i )</th>
<th>Link</th>
<th>( L_i )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( l_1 )</td>
<td>0.99</td>
<td>( l_8 )</td>
<td>0.98</td>
</tr>
<tr>
<td>( l_2 )</td>
<td>0.98</td>
<td>( l_9 )</td>
<td>1</td>
</tr>
<tr>
<td>( l_3 )</td>
<td>0.98</td>
<td>( l_{10} )</td>
<td>0.99</td>
</tr>
<tr>
<td>( l_4 )</td>
<td>1</td>
<td>( l_{11} )</td>
<td>0.99</td>
</tr>
</tbody>
</table>
Step 3: figure out the request diagram for application1. Based on $S_i$ obtained in Step2, servers, switches, and routers are figured out based on the actual network configuration, shown in figure 3. Note that if Service1 and Service2 are installed on different servers or the different routing rules are involved, then the diagram will be different.

In this case, request diagram concerns all the devices to support application1. But if the routing rules in Router1 are changed to deliver its data packages only to Router3, then the request diagram will be changed to another one without Router2.

Step 4: establish the transfer probabilities of the multi-branch nodes for request diagram for application1.

In this example system, the requests of application1 are sent to server1 with a probability of 0.8, and to server 3 with a probability of 0.2 (when the object file is not found on server1).

Similarly, the transfer probabilities of $l_i$ are 0.6 and 0.4, respectively. For the nodes with only one outgoing link, the transfer probability of the link is simply 1.

Step 5: calculate $R_i'$ and $R_i''$ for application1. Here the evaluation of $R_i'$ is explained in detail:

1) Add a state $C$ for application1 indicating that this application request is completed successfully. Derive matrix $Q_i$ from the reliabilities of correlative nodes and links as well as the transfer probabilities.

2) Compute the matrix $W_i$= $-Q_i$, and the value of its determinant $|W_i|$. $W_i$ is an upper triangular matrix here, and $|W_i|=1$.

3) Remove the first column and the last row from $W_i$ to get a new matrix $M_i$, then obtain the result $|M_i|$. $|M_i|$=0.86852.

4) The request reliability of application1 can be calculated as:

$$R_i' = (-1)^n |M_i| = (-1) \times -0.86852 = 0.86852$$

where, $n$ represents the number of nodes in the topology of figure 3, which is 9.

Calculate reliability $R_i''$ in the similar way. In this example, response diagram is the same as the request diagram with opposite directions. So we have $R_i'' = R_i' = 0.86852$. Thus, $R_i = R_i' \times R_i'' = 0.86852^2 = 0.75433$.

Step 6: Similarly, following step 2 to step 5, reliabilities of application2 and application3 can be evaluated as: $R_2=0.68800, R_3=0.69499$.

Step 7: calculate the network reliability as a weighted sum of all the single application reliabilities. The weights of the three applications are calculated as the proportion of their users. Thus the entire network application is calculated as:

$$R = \sum_{i=1}^{3} \omega_i \times R_i = 0.2 \times 0.75433 + 0.3 \times 0.68800 + 0.5 \times 0.69499 = 0.704761 .$$

5. Experiments and analysis

Further experiments are performed on the example network under different conditions to study the effects of component reliability and applications on the network reliability.

5.1. Experiment 1: Influence of component reliability on network reliability

Fig. 4. shows the change of the application reliability $R_a$, $R_b$, and network reliability $R$, when the reliability value of switch4, $N_s$ changes. Similarly, fig. 5. shows the effect of the change of reliability of switch5 $N_s$, on the reliabilities of single applications and the entire network.

Based on fig. 4 and fig. 5, we can see that $R_a$, $R_b$, $R_c$, and $R$ decrease as $N_s$ or $N_s$ decreases. In addition, switch4 is more important than switch5 to application1 and application2, because $R_a$ and $R_b$ reduce more rapidly in fig. 4 than in fig. 5. As shown through this example, our algorithm can facilitate the study of sensitivity or importance of different components to the network reliabilities.
Meanwhile, the reliability of a network can be totally different; network reliability has been studied and widely acknowledged. Server3, with a branch to Server1, has a greater reliability than the branch to Server3. This is reasonable because the branch to Server1 has a greater reliability than the branch to Server3.

The influence of component reliability on the overall network reliability has been studied and widely acknowledged. Meanwhile, the reliability of a network can be totally different when different applications are considered for the same network. Experiments performed in Sections 5.1 and 5.2 show that our evaluation method reflects the influence of not only components but also applications on the network reliability. This research is our first step for studying application-oriented reliability for communication networks with deterministic routings. It has provided another view of network reliability, which can reflect the users’ requirements better.

6. Conclusions and future work

Traditional network reliability algorithms mainly focus on network topology/connectivity while giving little or no consideration to applications running on the network. Thus results obtained using the traditional methods are not convincing enough for practical projects in enterprises because applications can affect the performance/reliability of a network greatly. A new application-centric network reliability concept and corresponding evaluation algorithm have been proposed in this paper. As shown through the case study and experiments, the algorithm considers the effects of both component reliabilities and applications in the network reliability evaluation.

Our future work will focus on (1) how to classify applications to reduce the computational overhead when the number of service is large; (2) how to optimize the algorithm to avoid the computational complexity caused by the excessive matrix order when the number of nodes related to a specific application is enormous; and (3) how to abstract more useful information about applications and components and incorporate it into the algorithm.

7. References


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